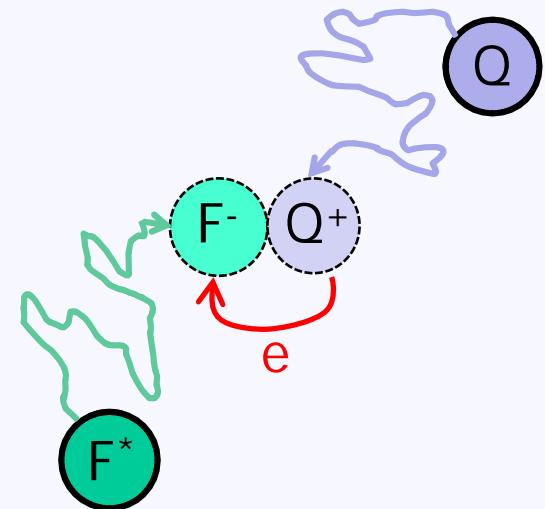


# Bimolecular electron transfer kinetics and solute diffusion in ionic liquids

- ❑ Motivation
- ❑ Quenching Basics & Initial Results
- ❑ More Sophisticated Interpretations
- ❑ Missing Dynamics

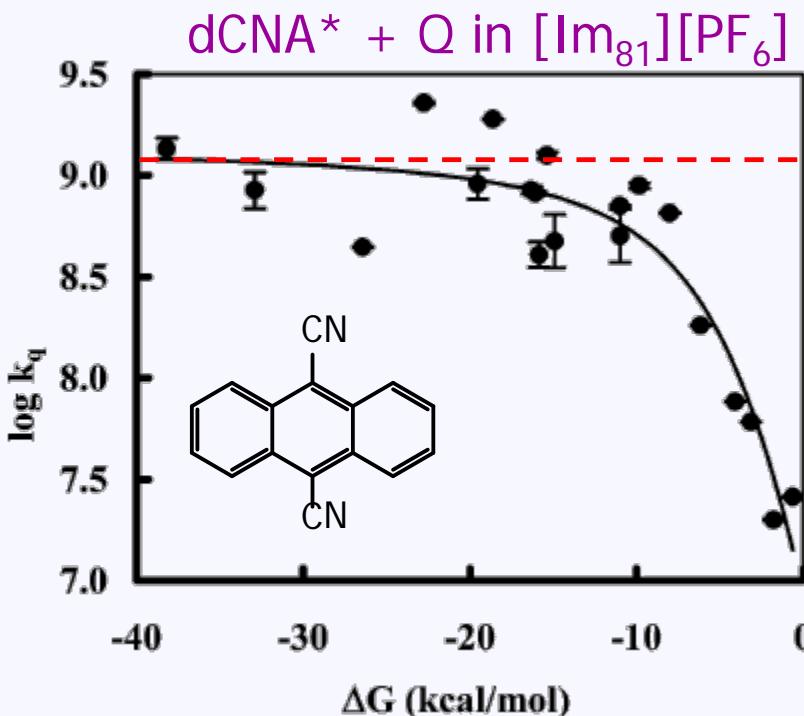


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The Pennsylvania State University

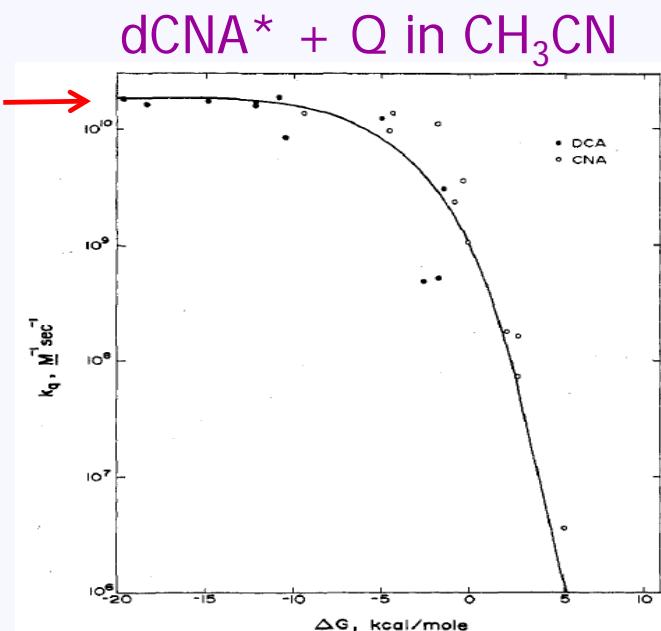


# Motivation

- Vieira & Falvey measured ET quenching of  $S_1$  dicyanoanthracene (dCNA) by 21 aromatic electron donors in 2 imidazolium ILs



$k_D$  →  
diffusion-limited rate constants



Eriksen & Foote, *J. Phys. Chem.* 82, 2859 (1978).

Viera & Falvey, *J. Phys. Chem. B* 111, 5023 (2007).

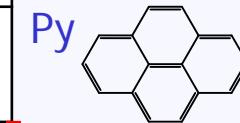
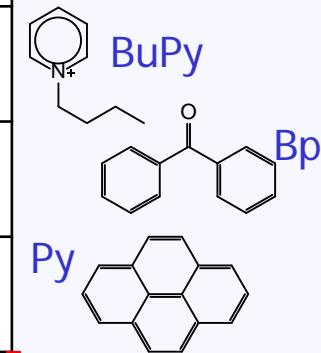
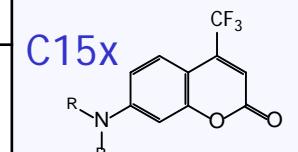
Solvent	$\eta/\text{cP}$	$k_D/M^{-1} \text{ s}^{-1}$
$[\text{Im}_{41}][\text{PF}_6]$	350	$1.4 \times 10^9$
$[\text{Im}_{81}][\text{PF}_6]$	570	$1.3 \times 10^9$
$\text{CH}_3\text{CN}$	0.34	$3.6 \times 10^{10}$

➤ compared to  $\text{CH}_3\text{CN}$ ,  $\eta$  in ILs is greater by  $10^3$  but  $k_D$  is only ~20-fold smaller

# Other Diffusion-Limited Rates

Reaction	IL	$k_{\text{obs}}/k_{\text{clc}}$	Technique	Ref.
dCNA <sup>*</sup> + D → dCNA <sup>-</sup> + D <sup>+</sup>	[Im <sub>n1</sub> ][PF <sub>6</sub> ] n=4,8	55, 98	SS fluor.	Falvey 2007
C15x <sup>*</sup> + DMA → C15x <sup>-</sup> + DMA <sup>+</sup>	DAF	1.5   60	ps   SS fluor.	Sarkar 2009
BuPy <sup>•</sup> + DQ → BuPy <sup>+</sup> + DQ <sup>•-</sup>	5 N & Pr ILs	3-9	radiolysis & ns TA	Neta 2003
<sup>3</sup> Bp <sup>*</sup> + Naph → Bp + <sup>3</sup> Naph <sup>*</sup>	5 Im ILs	2-8	ns TA	Gordon 2002
Py <sup>*</sup> + DMA → Py <sup>-</sup> + DMA <sup>+</sup>	4 Im ILs	1.3-2.8	SS & ps fluor.	Samanta 2007
I <sub>2</sub> <sup>-</sup> + I <sub>2</sub> <sup>-</sup> → I <sub>3</sub> <sup>-</sup> + I <sup>-</sup>	6 ILs	0.8-1.2	ns TA	Takahashi 2007
MV <sup>+</sup> + MV <sup>2+</sup> → MV <sup>2+</sup> + MV <sup>+</sup>	3 Im ILs	.21-.23	ESR lineshape	Grammp 2006
Ru(bpy) <sub>3</sub> <sup>*2+</sup> + MV <sup>2+</sup> → Ru(bpy) <sub>3</sub> <sup>3+</sup> + MV <sup>+</sup>	[Im <sub>41</sub> ][PF <sub>6</sub> ]	0.8	ns TA	Gordon 2000

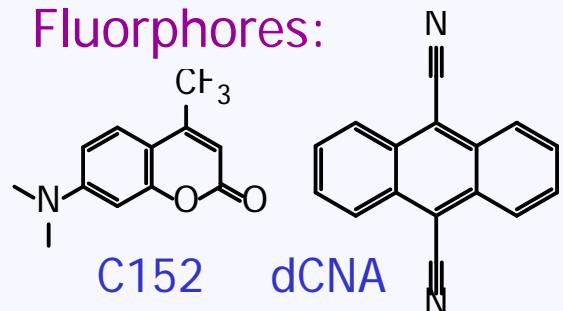
$$k_{\text{clc}} = \frac{4k_B T}{\eta}$$



➤ rapid diffusion? solute association?

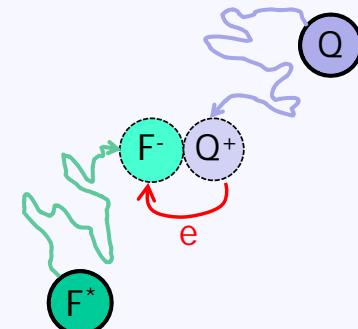
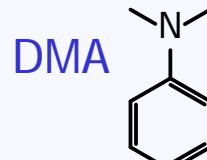
# Our Quenching Experiments

Fluorphores:



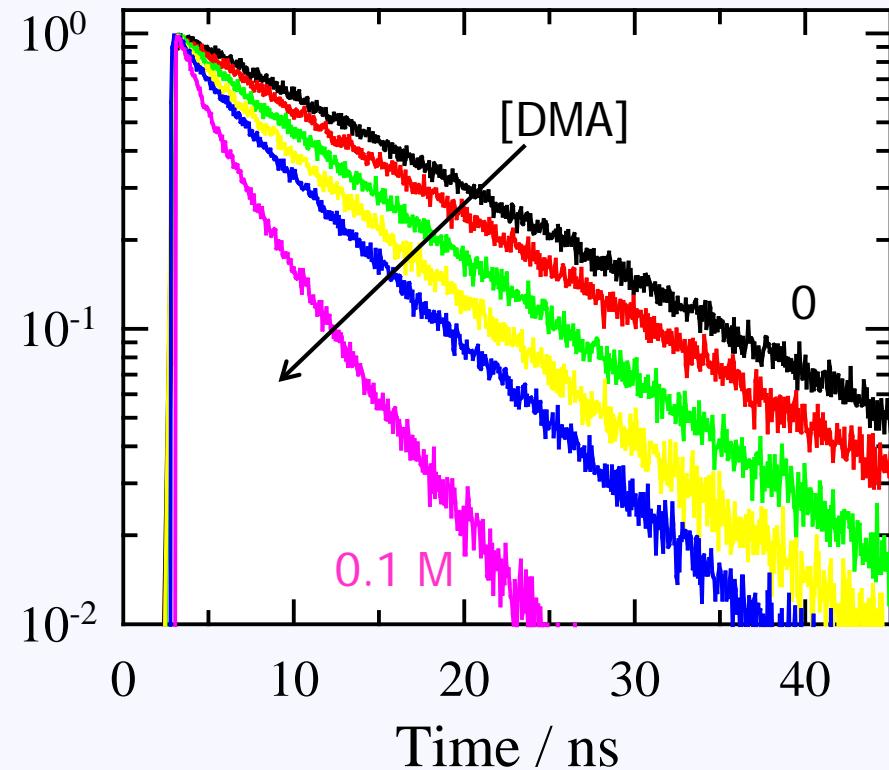
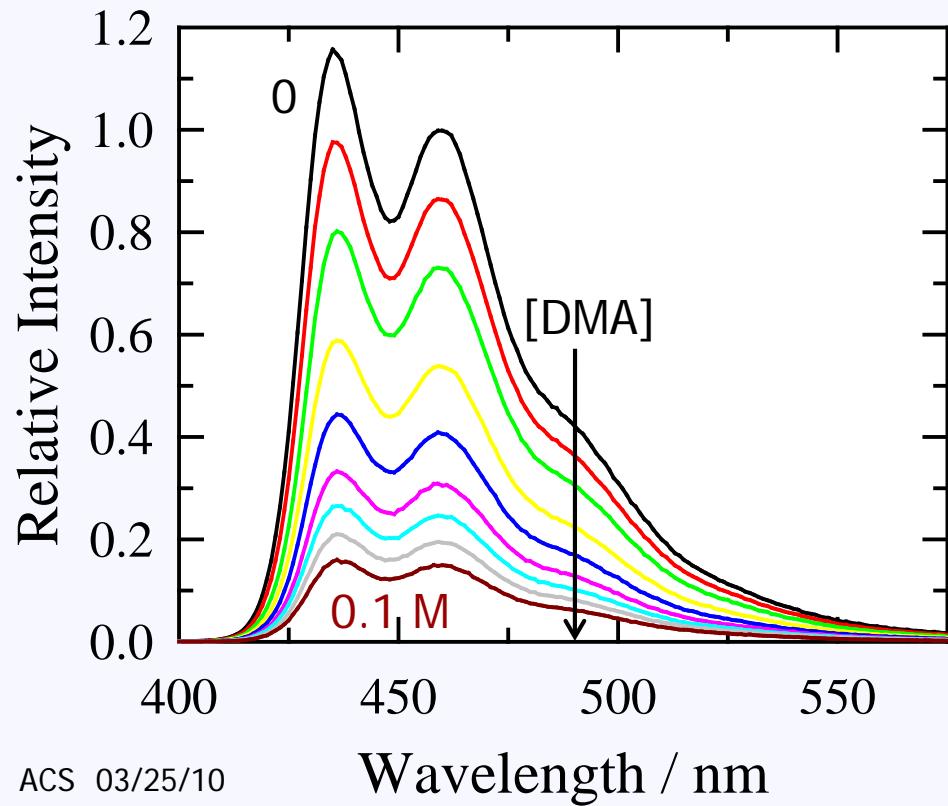
Quencher:

DMA



- ET mechanism
- solution & neat quencher data
- diffusion limited

Typical Data: dCNA+DMA in  $[\text{N}_{3111}][\text{Tf}_2\text{N}]$



# Some Basics: Stern-Volmer Kinetics & $k_q$

- assume quenching can be treated as a rate process:

$$\frac{d[F^*]}{dt} = k_0[F^*] + k_q[Q][F^*]$$

[F\*] - fluorophore concentration

[Q] - quencher concentration

$k_0$  - decay const. in absence of Q

$k_q$  - quenching rate constant

$$\frac{I(t)}{I(0)} = \frac{[F^*(t)]}{[F^*(0)]} = \exp\left\{- (k_0 + k_q[Q])t\right\}$$

emission  
decay

- this rate approach leads to the Stern-Volmer equation(s):

decay times

$$\frac{\tau_0}{\tau} = 1 + k_q \tau_0 [Q] \quad (\tau_0 = k_0^{-1})$$

SS intensities

$$\frac{I_0}{I} = 1 + k_q \tau_0 [Q]$$

O<sub>2</sub> Quenching of Tryptophan

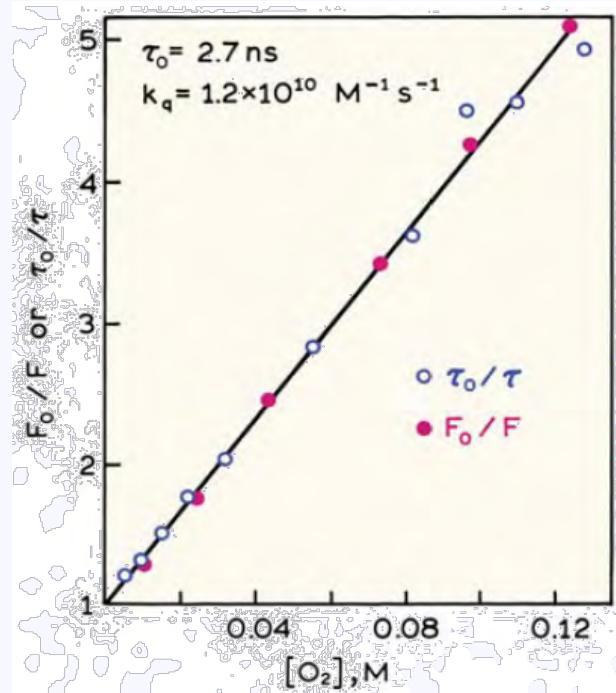
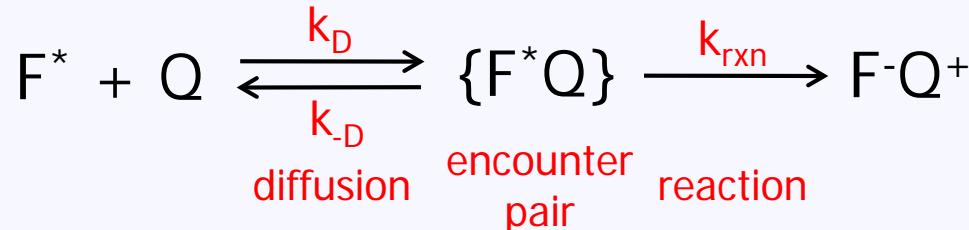


fig. from Lakowicz, *Principles of Fluorescence Spectroscopy* (Springer, 2006)

# $k_q$ at the Diffusion Limit

- envision quenching as a 2-step irreversible rate process:



- applying the SS approximation, for rapid reactions ( $k_{rxn} >> k_{-D}$ ), quenching is a pseudo-first order process with rate constant

$$k_q = k_D (1 + k_{-D} / k_{rxn})^{-1} \cong k_D$$

- $k_D$  can be modeled using the Smoluchowski approach [immobile F, independent Qs, continuum fluid,  $k_{rxn}(r) = \delta(R_{rxn})$ ] which, in the absence of a Q-F potential, provides the simple "Smoluchowski" eqn:

$$k_q = k_D = 4\pi(D_F + D_Q)R_{rxn}$$

D<sub>i</sub> – diffusion coefficient of i  
R<sub>rxn</sub> – reaction distance

## $k_q$ at the Diffusion Limit (cont.)

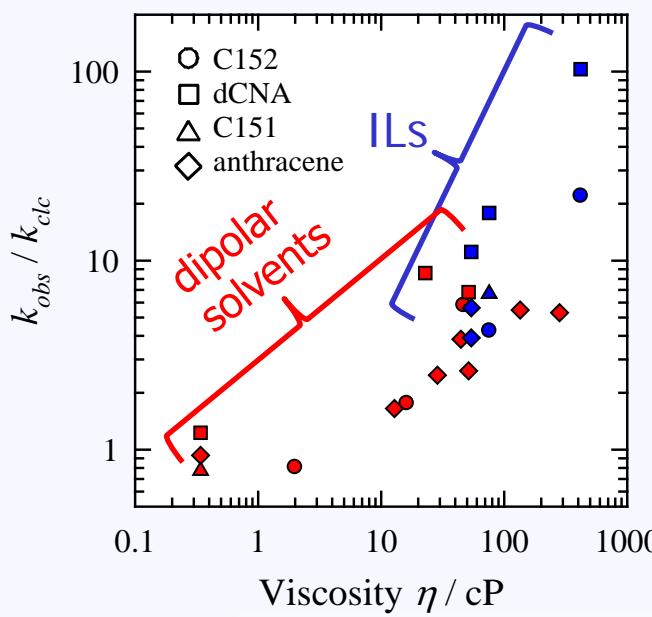
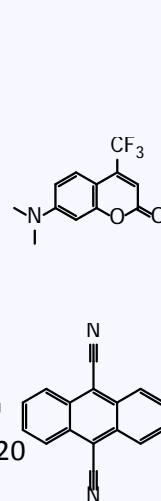
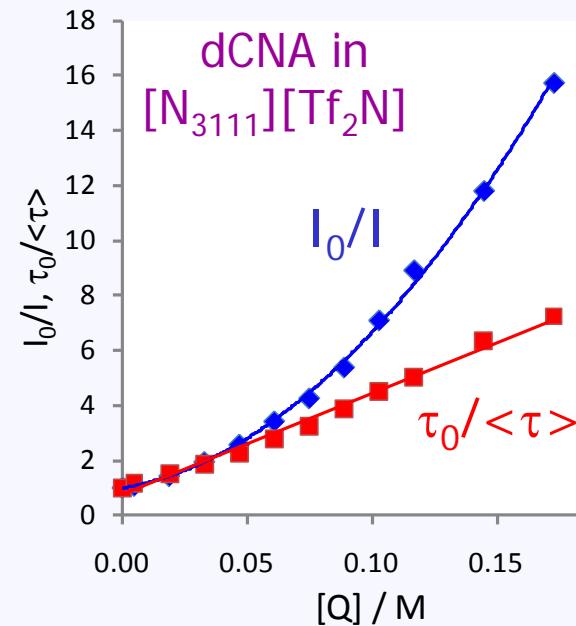
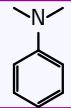
- finally, modeling the  $D_i$  using the Stokes-Einstein equation (slip BCs),

$$D_i = \frac{k_B T}{4\pi R_i \eta}$$

and assuming  $R_F \cong R_Q \cong R_{rxn}/2$ , one obtains the simplest prediction for a diffusion-limited reaction:

$$k_q = k_D \cong \frac{4k_B T}{\eta}$$

# Quenching Rates ( $Q = \text{C}_6\text{N}^+$ , 298 K)



$$\text{obs/clc} \equiv k_{obs} / (4k_B T / \eta)$$

$F^*$	solvent	$\eta / \text{cP}$	$k_{obs}$	$\tau_0 / \langle \tau \rangle$	$\text{obs}/\text{clc}$	$k_{obs}$	$\text{obs}/\text{clc}$
C152	acetonitrile	0.3	~350	~1	158	1	1
C152	$[\text{N}_{3111}][\text{Tf}_2\text{N}]$	76	6	10	21	16	16
C152	$[\text{P}_{14,666}][\text{Tf}_2\text{N}]$	418	5	22	10	43	43
dCNA	acetonitrile	0.3	357	1	349	1	1
dCNA	$[\text{Pr}_{31}][\text{Tf}_2\text{N}]$	54	20	11	34	18	18
dCNA	$[\text{N}_{3111}][\text{Tf}_2\text{N}]$	76	23	18	40	31	31
dCNA	$[\text{P}_{14,666}][\text{Tf}_2\text{N}]$	418	24	100	63	270	270
C152	ethylene glycol	16	13	2	56	9	9
C152	1,3-propanediol	47	12	6	25	12	12
dCNA	1,3-propanediol	23	39	9	109	24	24
dCNA	EG+Gly	51	13	7	33	17	17

$k_{obs}$  units  $10^{-8} \text{ M}^{-1} \text{ s}^{-1}$

- $k_q$  in ILs is 10-100× larger than predicted
- related to high viscosities in ILs

# Why the Deviations?

$$k_q = k_D \stackrel{?}{\cong} \frac{4k_B T}{\eta}$$

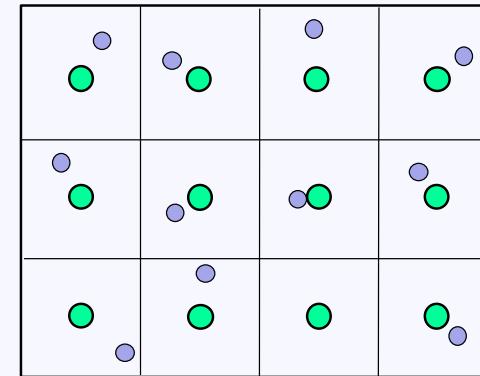
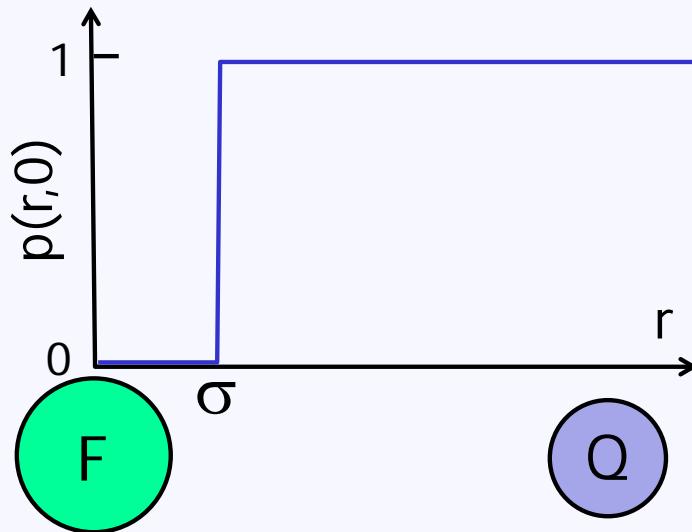
Three approximations might be inappropriate for these ET reactions in ILs:

1. neglect of the transient portion of the reaction  
(and treatment as a simple rate process)
2. assuming a contact model for the ET process
3. using Stokes-Einstein hydrodynamic predictions

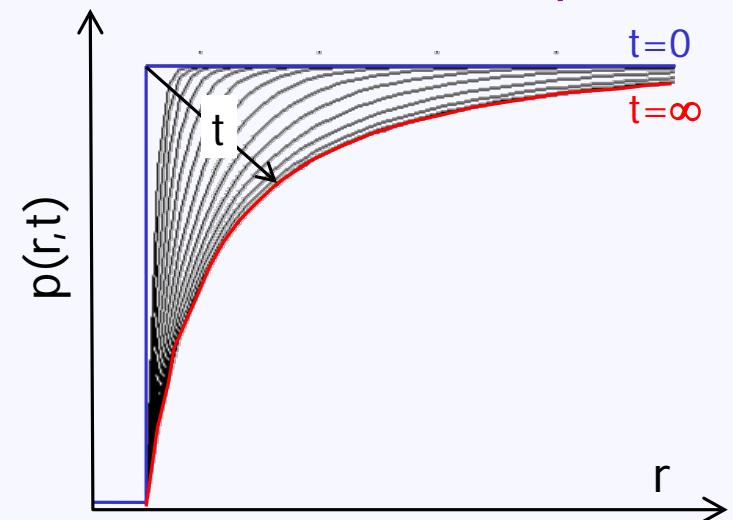
# The Transient Effect

- diffusion-influenced reactions can be described by rate laws only after a transient time during which  $k_q = k(t)$

The F-Q Spatial Distribution



Time Evolution of  $p(r,t)$



- increasing  $\eta$  lengthens the transient time thereby increasing its relative importance

# A More Complete Analysis

$$\frac{\partial}{\partial t} p(r,t) = \left[ \frac{1}{r^2} \frac{\partial}{\partial r} r^2 D \frac{\partial}{\partial r} - \kappa(r) \right] p(r,t)$$

reaction model

spherically symmetric diffusion equation for  $p(r,t)$

$$k(t) = 4\pi \int_{\sigma}^{\infty} \kappa(r) p(r,t) r^2 dr$$

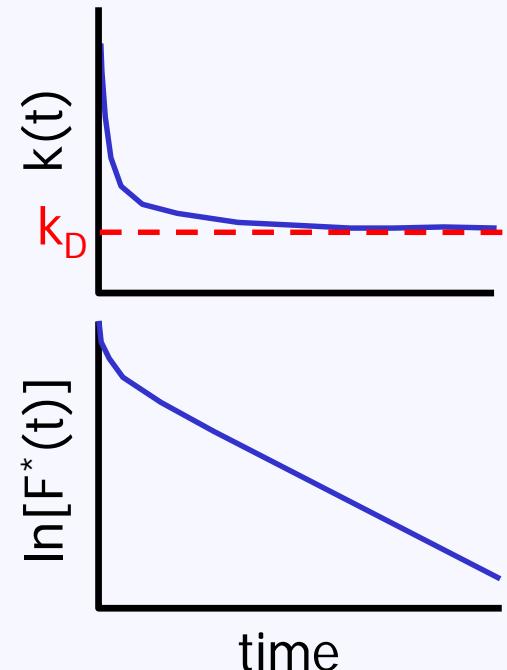
time-dependent rate constant

$$[F^*(t)] = [F^*(0)] \exp \left\{ -\frac{t}{\tau_0} - [Q] \int_0^t k(t') dt' \right\}$$

Smoluchowski (1917):  $\kappa(r)=\infty$  for  $r=\sigma$

$$k(t) = k_D \left\{ 1 + \sqrt{\frac{\sigma^2}{\pi D t}} \right\} \quad k_D = 4\pi\sigma D = 4\pi\sigma(D_F + D_Q)$$

$$\frac{[F^*(t)]}{[F^*(0)]} = \exp \left\{ -\frac{t}{\tau_0} - [Q] \left[ k_D t + 8\sigma^2 \sqrt{\pi D t} \right] \right\}$$



# Diffusion Equation Modeling

$$\frac{\partial}{\partial t} p(r,t) = \left[ \frac{1}{r^2} \frac{\partial}{\partial r} r^2 D(r) g(r) \frac{\partial}{\partial r} \frac{1}{g(r)} - \kappa(r) \right] p(r,t)$$

$p(r,t)$  – F\*-Q pair distribution function

$g(r)$  – equilibrium F-Q pair distribution function

\*  $\kappa(r)$  – distance-dependent reaction rate \*

$D(r)$  – diffusion coefficient (distance dependent)

Smoluchowski  
Collins & Kimball  
Fixman  
Szabo  
Tachiya  
Burshtein  
⋮

Dudko & Szabo<sup>1</sup> (2005): approximate analytic results  
for arbitrary  $\kappa(r)$  &  $g(r)$

$$k(t) = k(\infty) [1 + \alpha_1 e^{-\gamma_1^2 t} erfc(\sqrt{\gamma_1^2 t}) + \alpha_2 e^{-\gamma_2^2 t} erfc(\sqrt{\gamma_2^2 t})]$$

# An Electron Transfer Model for $\kappa(r)$

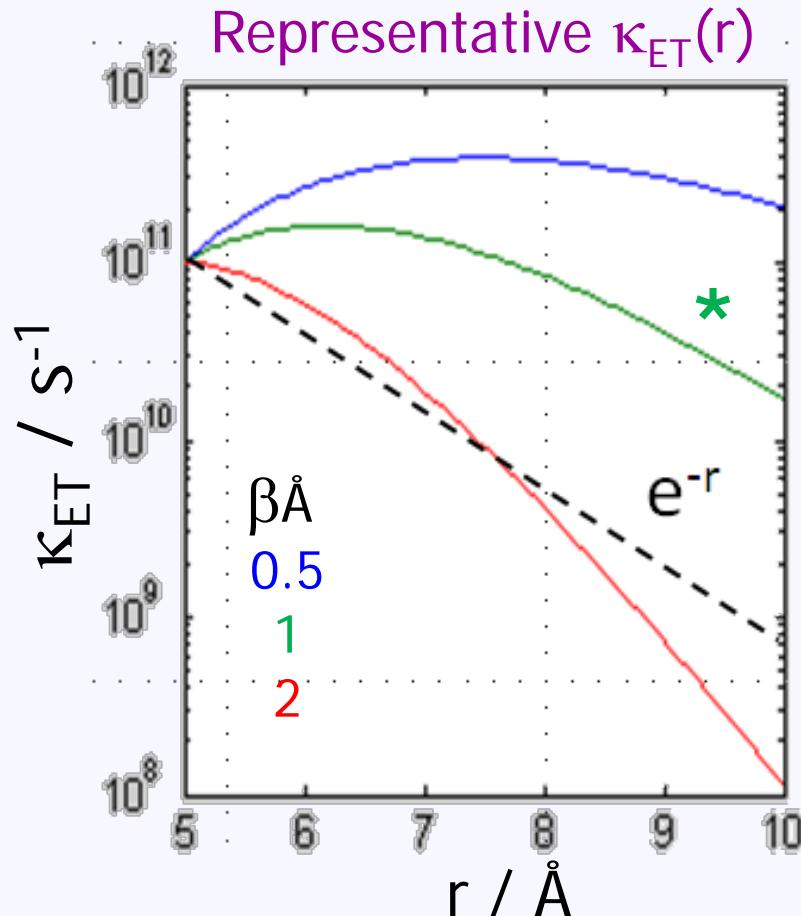
- use classical Marcus theory to estimate distance-dependent reaction rate  $\kappa(r)$ :

$$\kappa_{ET}(r) = \frac{V^2 e^{-\beta(r-r_0)}}{h\sqrt{4\pi\lambda k_B T}} \exp\left\{-\frac{(\Delta G + \lambda)^2}{4\lambda k_B T}\right\}$$

$$\lambda_{sol}(r) = e^2 \left\{ \frac{1}{2r_D} + \frac{1}{2r_A} - \frac{1}{r_{DA}} \right\} \left\{ \frac{1}{n^2} - \frac{1}{\varepsilon} \right\}$$

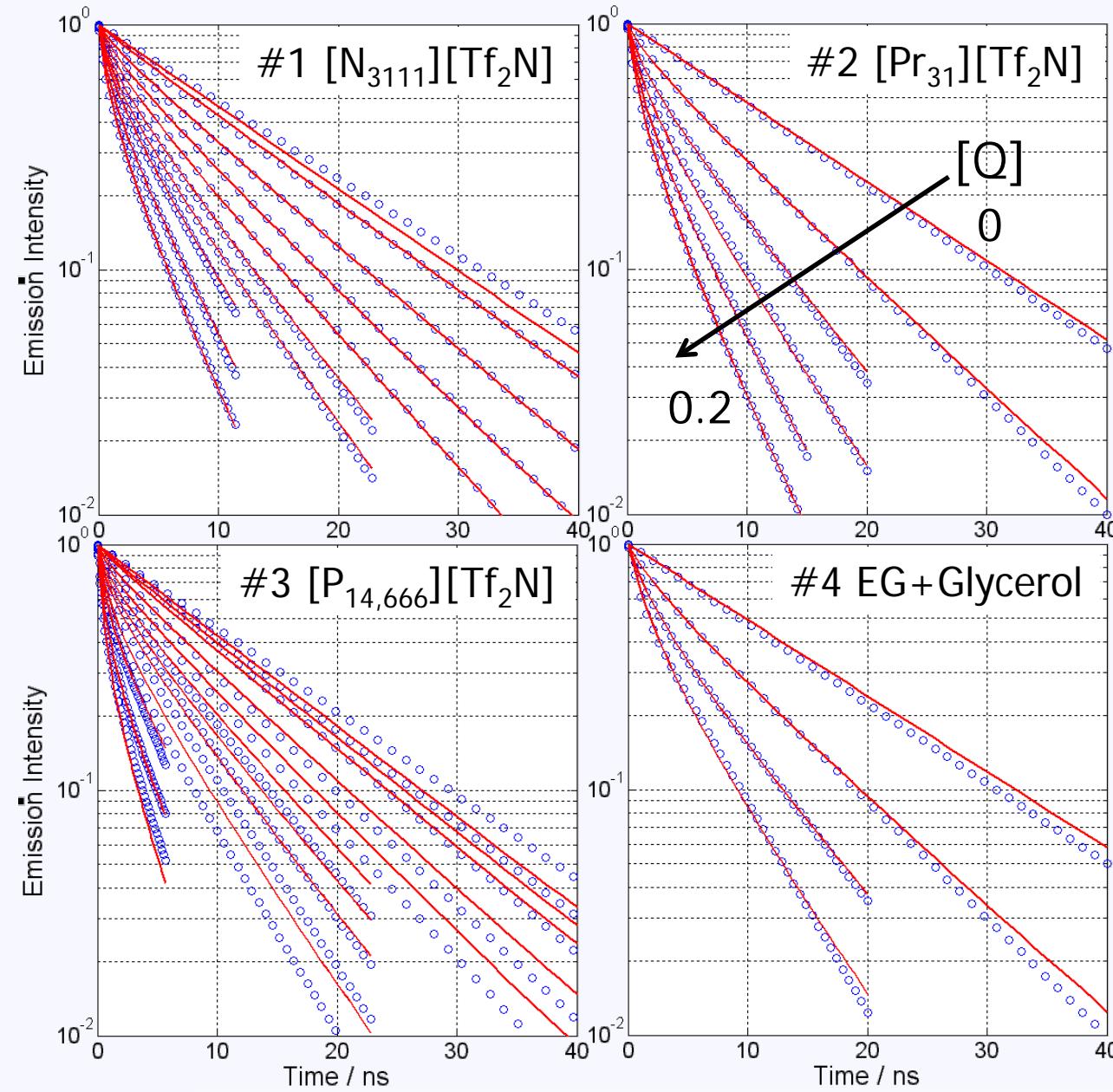
$$\Delta G(r) = \Delta G_0 - \frac{e^2}{\varepsilon r_{DA}}$$

$$\Delta G_0 = E(D/D^+) - E(A/A^-) - E_{00}$$



similar  $\kappa_{ET}(r)$  modeling also by Fayer, Tachiya, Burshtein, Grammp

# Fitting Emission Decays – dCNA+DMA



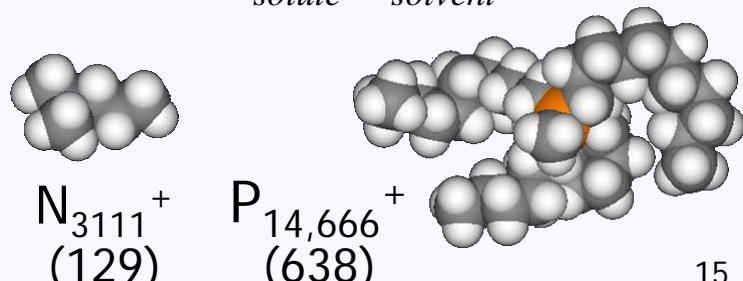
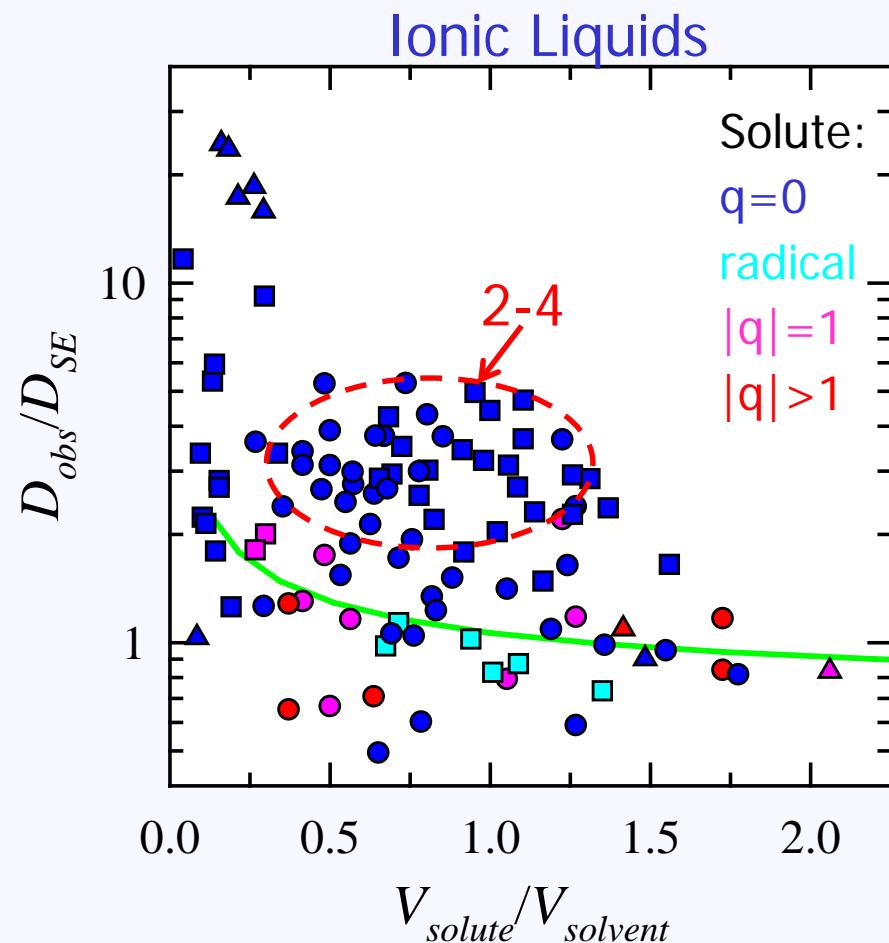
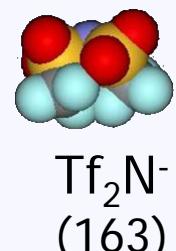
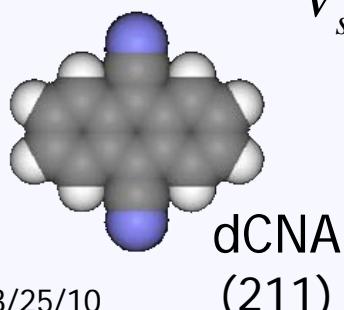
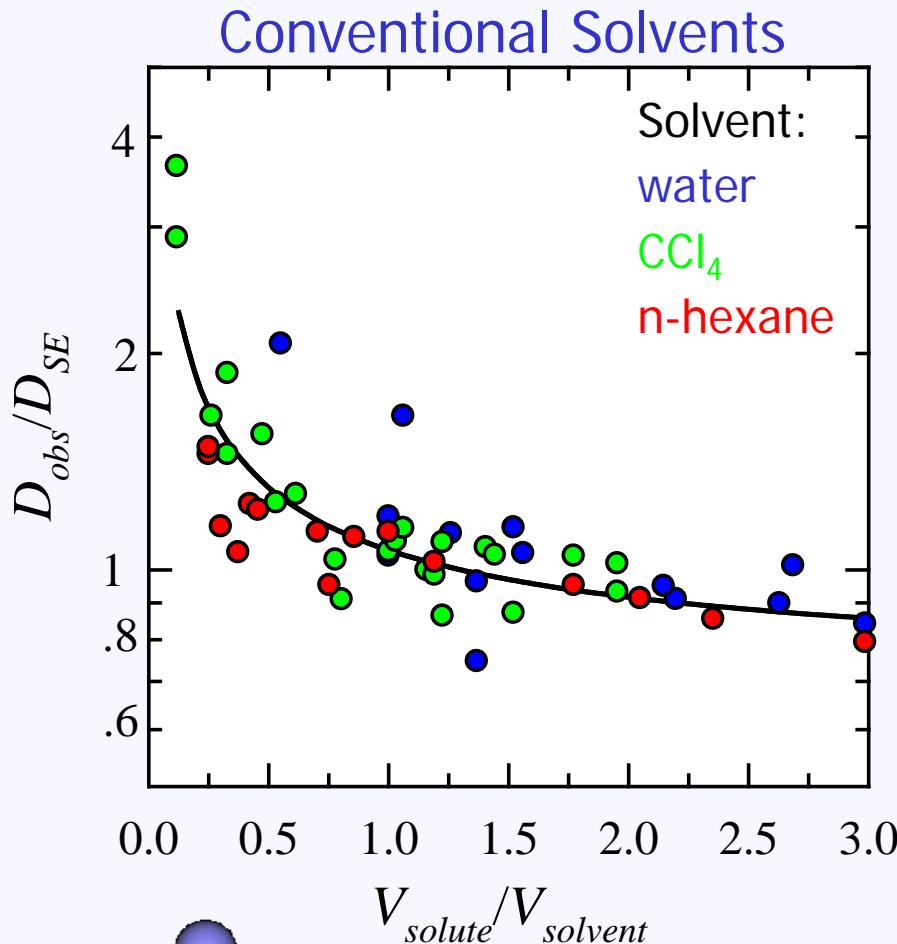
## Fixed Parameters

$$\begin{aligned}\Delta G^0 &= -1.0 \text{ eV} \\ \beta &= 1.0 \text{ \AA}^{-1} \\ \lambda_{in} &= 0.3 \text{ eV} \\ g_{max} &= 2.0 \\ r_0 &= 6.5 \text{ \AA} \\ \varepsilon &= 35, n_D = 1.4\end{aligned}$$

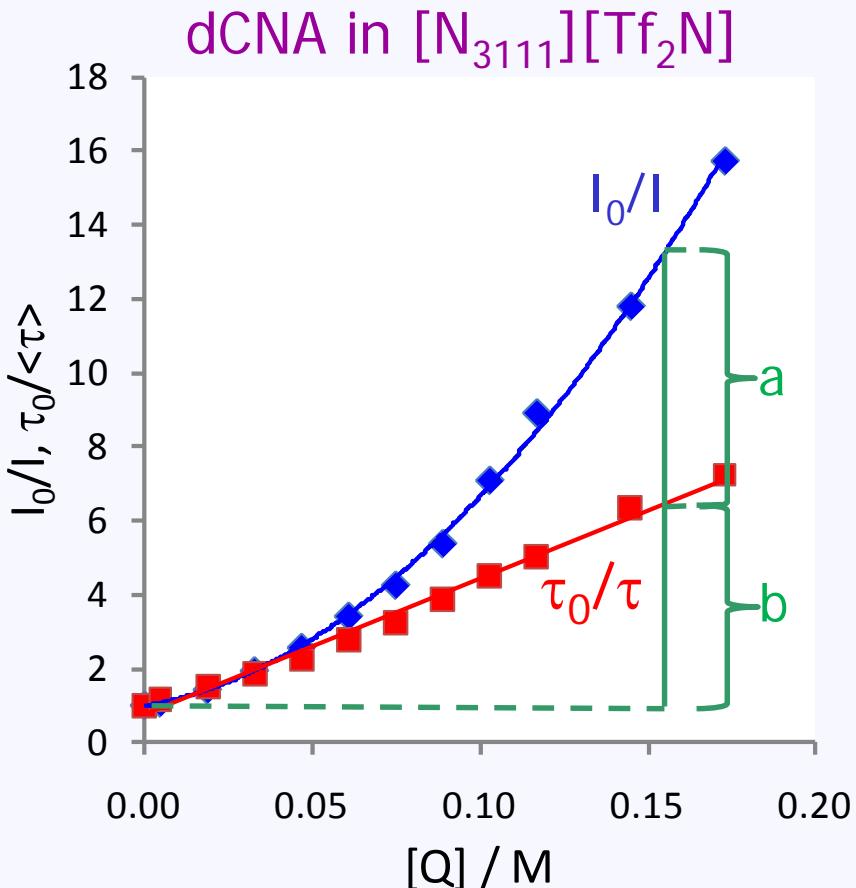
## Variable Parameters

#	$V_{el}$ $/cm^{-1}$	$D_{opt}$ $/D_{SE}$
1	66	5
2	58	3
3	(75)	16
4	48	2

# Solute Diffusion Coefficients & SE



# "Static" Quenching



% Missed by TCSPC ( $[Q] = .1 \text{ M}$ )

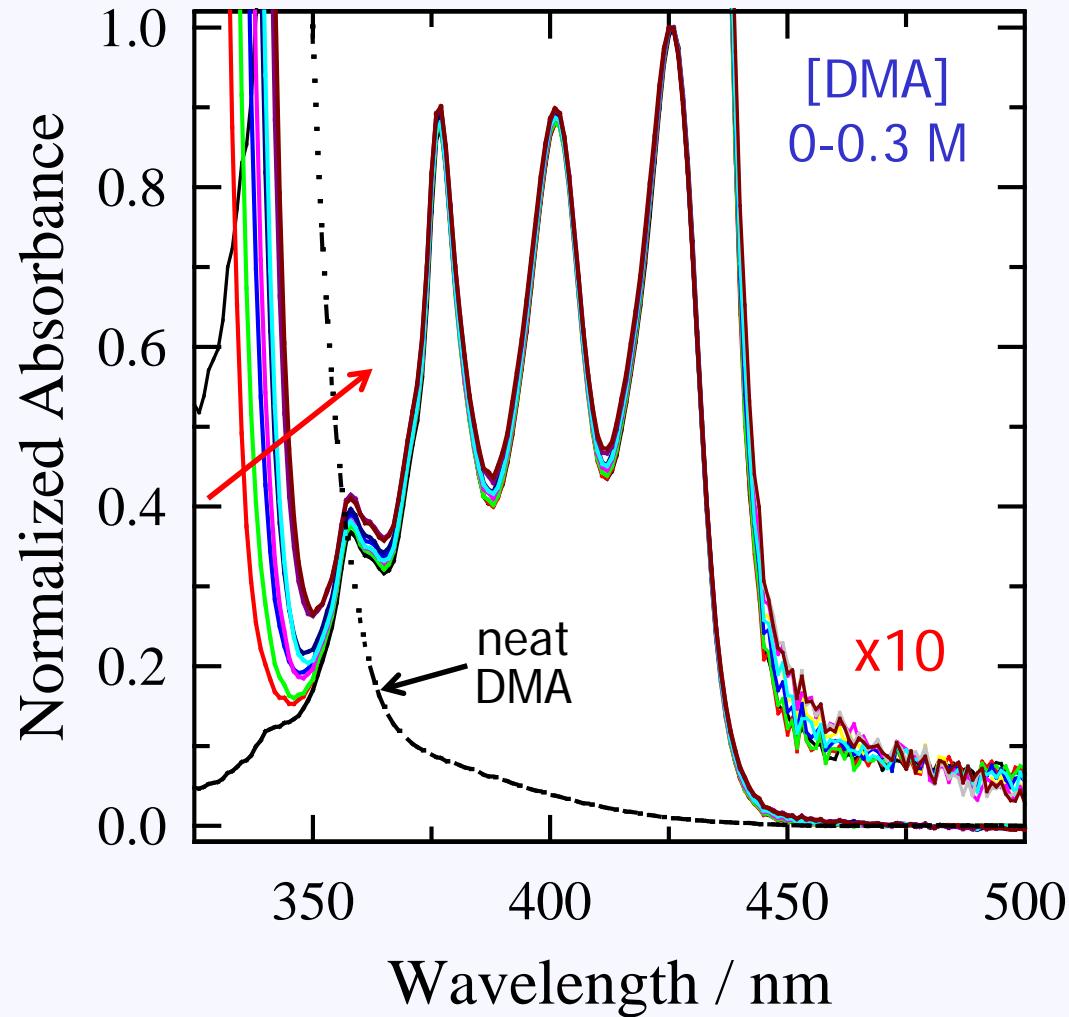
$F^*$	solvent	$\eta / \text{cP}$	% missed
C152	$[N_{3111}][Tf_2N]$	76	73
C152	$[P_{14,666}][Tf_2N]$	418	49
dCNA	$[Pr_{31}][Tf_2N]$	54	39
dCNA	$[N_{3111}][Tf_2N]$	76	42
dCNA	$[P_{14,666}][Tf_2N]$	418	61
C152	ethylene glycol	16	78
C152	1,3-propanediol	47	49
dCNA	1,3-propanediol	23	62
dCNA	EG+Gly	51	60

$$\% \text{ missed} = 100 \times a/(a+b)$$

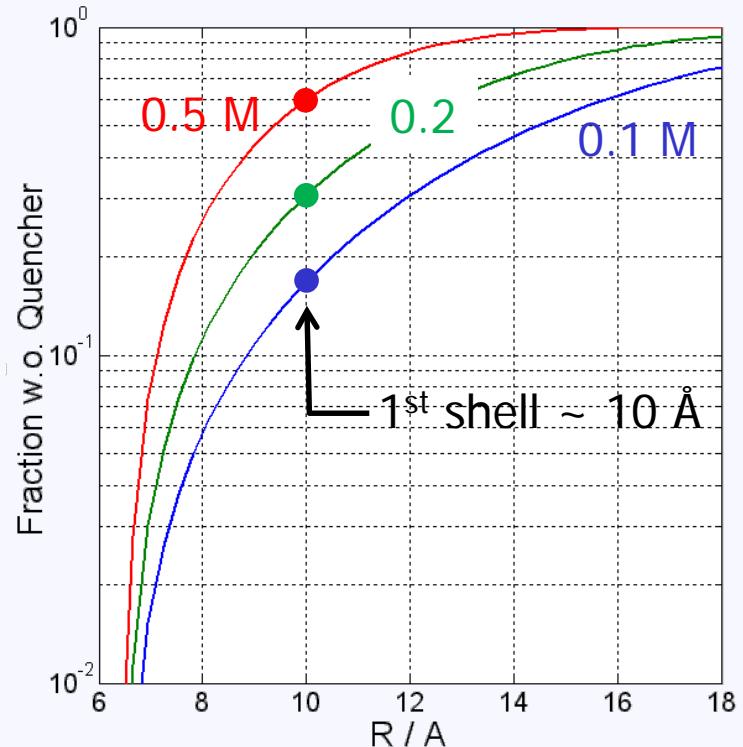
- TCSPC indicates substantial <5 ps ET even at  $[Q]=0.1 \text{ M}$
- for this reason SS Stern-Volmer analysis greatly exaggerates  $k_D$

# Ground-State Association?

Absorption: dCNA/[N<sub>3111</sub>][Tf<sub>2</sub>N]

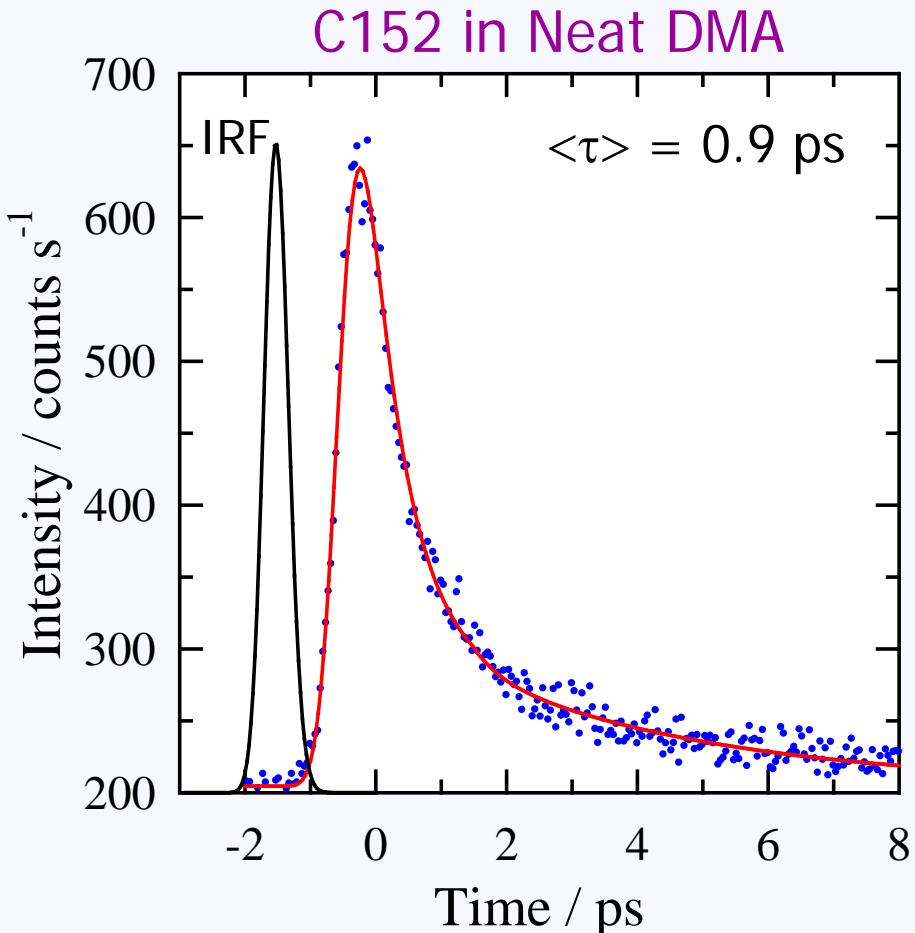


Estimated F\*-Q Probabilities

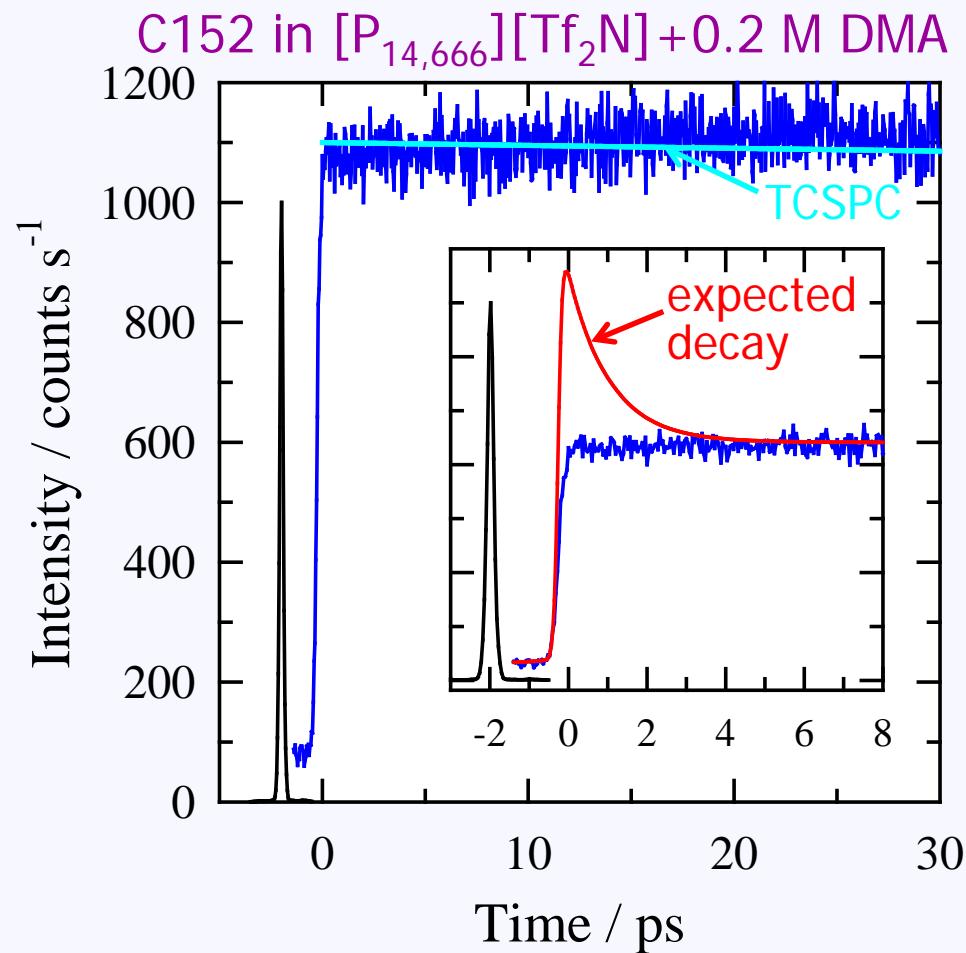


# Ultrafast Quenching Component

- fluorescence upconversion experiments, IRF = 200-300 fs



Yoshihara & Co (1995):  $\langle\tau\rangle = 0.71 \text{ ps}$   
Castner & Cave (2000):  $\langle\tau\rangle = 0.92 \text{ ps}$



➤ in 0.2 M DMA 50% of emission decay is faster than 100 fs?

# Summary & Outlook

- we've begun systematic fluorescence measurements of diffusion-limited electron transfer reactions in ILs
- diffusion-limited rates are much larger than estimates based on simple Smoluchowski prediction  $k_D = 4k_B T / \eta$
- several effects contribute at high  $\eta$ :
  - time-dependent rate [ $k(t)$ ] contributions
  - long-range electron transfer [ $\kappa(r)$ ]
  - $D$  larger than SE predictions
- substantial "static" quenching ~50% at 0.1 M
  - no evidence for complex formation
  - quenching faster than 100 fs
- behavior is not necessarily unique to ILs

# Acknowledgements



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Gary Baker (ORNL)



Min Liang

